# **Ultimate Circular Motion and Gravitation Assignment (16%)**

# **Key Formulae:**

$$T = \frac{1}{f}$$

$$T = \frac{1}{f}$$
  $a_c = \frac{v^2}{r} = \frac{4\pi^2 r}{T^2}$   $F = G \frac{m_1 m_2}{r^2}$   $E_p = -G \frac{m_1 m_2}{r}$ 

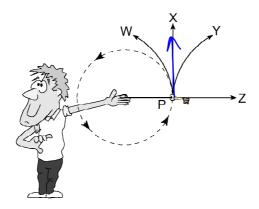
$$F = G \frac{m_1 m}{r^2}$$

$$E_p = -G \frac{m_1 m_2}{r}$$

0108

1.

The diagram shows a student "twirling" a car key in a circular path on the end of a string.



If the string snaps at P, which path will the keys follow?







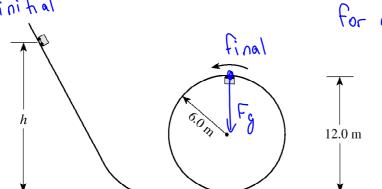
2.

An athlete runs, at a constant speed, around a circle of radius 5.0 m in 12 s. What are the athlete's speed and acceleration?

	SPEED	MAGNITUDE OF ACCELERATION
A.	0.42 m/s ×	0.22 m/s <sup>2</sup>
B.	0.42 m/s	1.4 m/s <sup>2</sup>
C.	2.6 m/s ✓	0.22 m/s <sup>2</sup>
D.	2.6 m/s 🗸	1.4 m/s <sup>2</sup>

$$\alpha = 4\pi^2\Gamma = 1.1$$

A frictionless 3.0 kg cart rolls down an incline, and then "loops the loop."



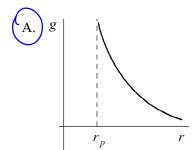
For minimum, + g = Fc Mg = MV2

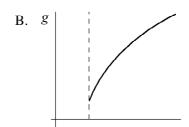
Diagram not to scale

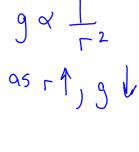
From what minimum height, h, should the cart be released so that it does not fall off the PE; + KE; = PE, + KE. circular track?

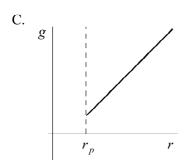
4.

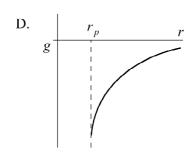
Which graph best shows how the gravitational field strength, g, varies with the distance, r, from the centre of a planet?  $(r_p)$  is the radius of the planet.











6.

A satellite is in a stable circular orbit around the earth. Another satellite in a stable circular orbit at a greater altitude must have

- A. a smaller speed and a shorter period.
- (B) a smaller speed and a longer period.
- C. a greater speed and a shorter period.
- D. a greater speed and a longer period.

Which of the following could represent the kinetic energy, the gravitational potential energy and the total energy for an orbiting satellite in a stable circular orbit?

	KINETIC ENERGY	GRAVITATIONAL POTENTIAL ENERGY	TOTAL ENERGY
(A.)	40 000 J <b>/</b>	−80 000 J 📝	-40 000 J
B.	40 000 J	40 000 J	80 000 J
C.	80 000 J	40 000 J	120 000 J
D.	80 000 J	-40 000 J	40 000 J

A spacecraft of mass 470 kg rests on the surface of an asteroid of radius 1 400 m and mass  $2.0 \times 10^{12}$  kg. How much energy must be expended so that the spacecraft may rise to a height of 2 800 m above the surface of the asteroid? (7 marks)

0106

8.

A car travels at 25 m/s along a horizontal curve of radius 450 m. What minimum coefficient of friction is necessary between its tires and the road in order for the car not to skid?

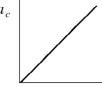
- 0.14 В. 0.54
- C. 0.72
- D. 1.4

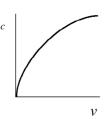
Hara Fc Mag = ofv<sup>2</sup>

 $1 = \frac{v^2}{95} = .142$ 

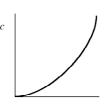
9.

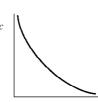
In a series of test runs, a car travels around the same circular track at different velocities. Which graph best shows the relationship between its centripetal acceleration,  $a_c$ , and its velocity, v?





 $a_c$ 





parabola

10.

FBD

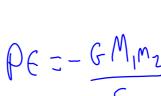
Tarzan, of mass 85 kg, holds on to a horizontal vine of length 8.0 m and jumps off a cliff. What is the tension force in the vine as Tarzan passes the lowest point of his circular path?

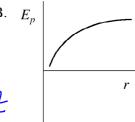


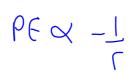
be! = Ket - used A!

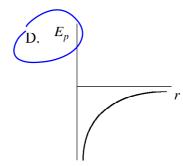
Which graph shows gravitational potential energy plotted as a function of distance r from the centre of the earth?

A.  $E_p$ 









#### 12.

How much work must be done to lift a  $4.00 \times 10^4$  kg object from Earth's surface to a heighhof

B. 
$$1.18 \times 10^{11} \text{ J}$$

$$C = 2.39 \times 10^{12} \text{ J}$$

D. 
$$5.32 \times 10^{13} \text{ J}$$

$$= -\frac{GM_1M_2}{\Gamma_0} - \frac{GM_1M_2}{\Gamma_0}$$

$$= -2.388 \times 10^{12} + 2.501 \times 10^{12}$$

$$= 1.12 \times 10^{11}$$

- 13. An 884 kg satellite in orbit around a planet has a gravitational potential energy of  $-5.44 \times 10^{10} \, \text{J}$ . The orbital radius of the satellite is  $8.52 \times 10^6 \, \text{m}$  and its speed is  $7.84 \times 10^3 \, \text{m/s}$ .
- a) What is the mass of the planet?

(3 marks)

b) What is the kinetic energy of the satellite?

(2 marks)

c) What is the total energy of the satellite?

(2 marks)

a) 
$$F_g = F_c$$

$$\frac{GMm}{r^2} = \frac{m^2 v^2}{K} \Rightarrow M = \frac{v^2 \Gamma}{(5 - (7.84 v 10^3)^2 (8.52 v 10^6))}$$

$$M_{planet} = 7.85 v 10^{24} kg$$

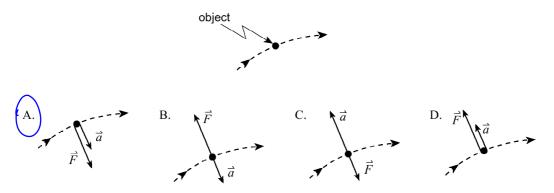
6) 
$$kE = \frac{1}{2}mv^2 = \frac{1}{2}PE$$
, but positive = 2.72 +10 J

c) 
$$TE = PE + KE = -5.44 \times 10^{10} + 2.72 \times 10^{10}$$
  
= -2.72 × 10<sup>10</sup> J

#### 0101

14.

Which vector diagram best represents the acceleration,  $\vec{a}$ , and force,  $\vec{F}$ , for an object travelling along a circular path?

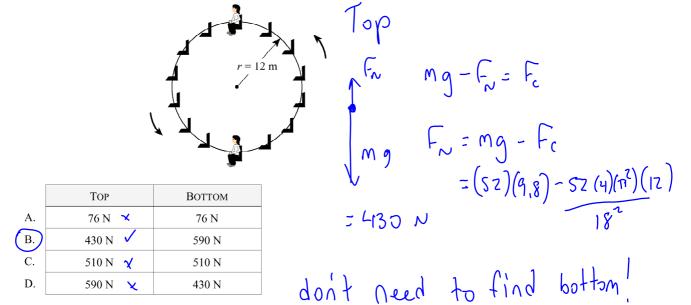


15.

An object travels along a circular path with a constant speed  $\nu$  when a force F acts on it. How large a force is required for this object to travel along the same path at twice the speed  $(2\nu)$ ?

A. 
$$\frac{1}{2}F$$
B.  $F$ 
C.  $\frac{2F}{0.4F}$ 
 $\frac{1}{2}F$ 
 $\frac{1}$ 

The diagram shows a 52 kg child riding on a Ferris wheel of radius 12 m and period 18 s. What force (normal force) does the seat exert on the child at the top and bottom of the ride?

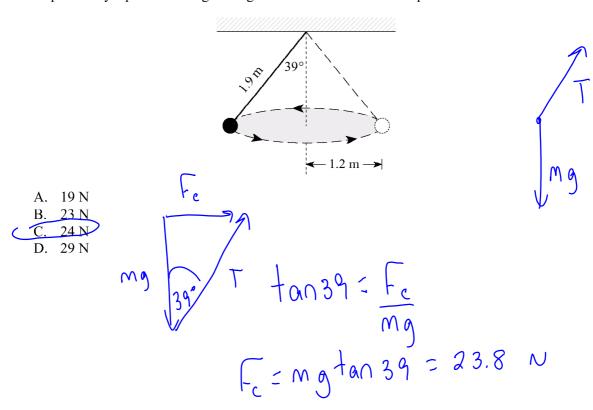


The equation  $E_p = mgh$ , in which g is 9.8 m/s<sup>2</sup>, can not be used for calculating the gravitational potential energy of an orbiting Earth satellite because

- A. the Earth is rotating.
- B. of the influence of other astronomical bodies.
- C. the Earth's gravity disappears above the atmosphere.
- (D.) the Earth's gravitational field strength varies with distance.

18.

The diagram shows an object of mass 3.0 kg travelling in a circular path of radius 1.2 m while suspended by a piece of string of length 1.9 m. What is the centripetal force on the mass?



a) Mars has a mass of  $6.37 \times 10^{23}$  kg and a radius of  $3.43 \times 10^6$  m. What is the gravitational

b) What thrust force must the rocket engine of a Martian lander exert if the 87.5 kg spacecraft is to accelerate upwards at 1.20 m/s<sup>2</sup> as it leaves the surface of Mars?

#### 0008

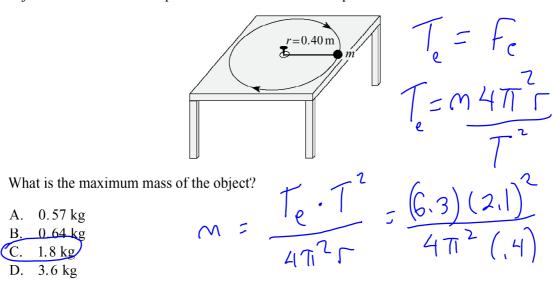
#### 20.

A car travels at a uniform speed through a level circular curve in the road. Which of the following correctly describes the magnitude of the acceleration, velocity and force acting on the car?

$\sim$	MAGNITUDE OF ACCELERATION	MAGNITUDE OF VELOCITY	MAGNITUDE OF FORCE
(A.)	constant √	constant /	constant 🗸
B.	constant 🗸	changing 🟏	changing 🗸
C.	constant	changing 🔨	constant
D.	changing 🗸	changing 🛪	changing 🗸

#### 21.

An object is attached to a string that can withstand a maximum tension force of 6.3 N. The object travels in a circular path of radius 0.40 m with a period of 2.1 s.



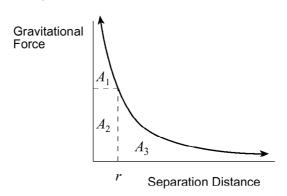
#### 22.

A 65 kg pilot in a stunt plane performs a vertical loop with a 700 m radius. The plane reaches a speed of 210 m/s at the bottom of the loop. What is the upward force on the pilot at the bottom of the loop?

$$\frac{FBO}{\int F_N} = F_N - mg = F_C$$

$$\int_{\Gamma_N} F_N = mg + mv^2 = 4.73 \times 10^3 N$$

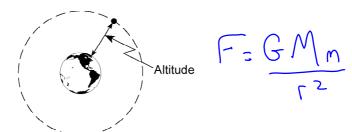
Which of the indicated areas of the graph represent the work needed to send an object from separation distance r to infinity?



- A.  $A_1 + A_2$

#### 24.

A satellite experiences a gravitational force of 228 N at an altitude of  $4.0 \times 10^7$  m above Earth.



this satellite?  $M = \frac{1}{GM} = \frac{(4x15^{1}+6.38x10^{6})^{2}(228)}{(6.67x15^{11})(5.98x10^{24})}$ What is the mass of this satellite?

- A. 23 kg
- B. 650 kg
- C. 910 kg

25.

Ď. 1 200 kg

570 kg satellite orbits a planet in a circle of radius 
$$5.94 \times 10^6$$
 m. Relative

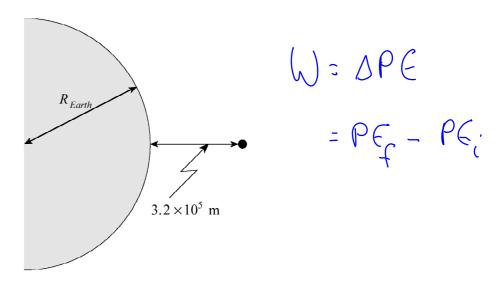
A 1 570 kg satellite orbits a planet in a circle of radius  $5.94 \times 10^6$  m. Relative to zero at infinity the gravitational potential energy of this satellite is  $-9.32 \times 10^{11}$  J. What is the mass of the planet?

- A.  $5.29 \times 10^{25} \text{ kg}$  $8.31 \times 10^{28} \text{ kg}$
- C.  $3.14 \times 10^{31}$  kg
- D.  $4.93 \times 10^{34} \text{ kg}$

$$PE = -\frac{GMm}{PE} = -\frac{(5.94 \times 10^{6})(-9.32 \times 10^{11})}{(6.67 \times 10^{-11})(1575)}$$

$$M = 5.3 \times 10^{25} \text{ kg}$$

A  $4.00 \times 10^3$  kg object is lifted from the earth's surface to an altitude of  $3.2 \times 10^5$  m. How much work does this require? (7 marks)



(Diagram not to scale.)

$$W = \frac{-GM_{1}M_{2}}{f_{2}} - \frac{-GM_{1}M_{2}}{f_{1}}$$

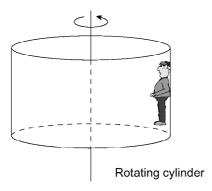
$$W = \frac{(-6.67 \times 10^{-11})(5.98 \times 10^{24})(4 \times 10^{3})}{(3.2 \times 10^{5} + 6.38 \times 10^{6})} + \frac{(6.67 \times 10^{-11})(5.98 \times 10^{24})(4 \times 10^{3})}{6.38 \times 10^{6}}$$

$$W = -2.38 \times 10^{11} + 2.50 \times 10^{11}$$
  
 $W = 1.21 \times 10^{10}$ 

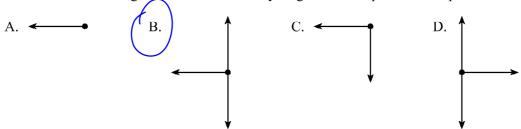
#### 0006

#### 27.

In a popular amusement park ride, a large cylinder is set in rotation. The floor then drops away leaving the riders suspended against the wall in a vertical position as shown.



Which of the following is the correct free-body diagram for the person at the position shown?



#### 28.

A 0.500 kg ball is swung in a horizontal circle of radius 1.20 m with a period of 1.25 s. What is the centripetal force on the ball?

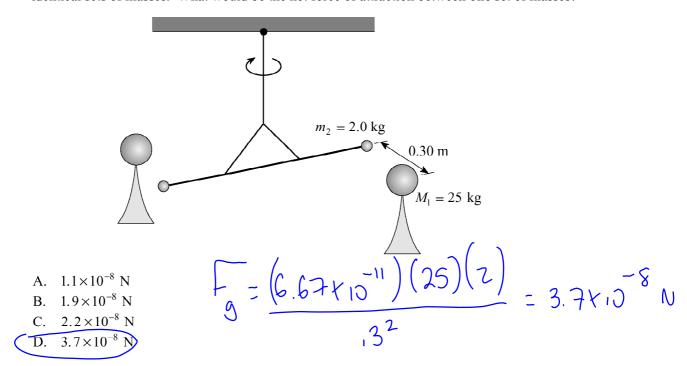
B. 15.2 N C. 18.9 N D. 30.3 N		FC=MAITT	15.2 N
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#### 29.

A rock drops from a very high altitude towards the surface of the moon. Which of the following is correct about the changes that occur in the rock's mass and weight?

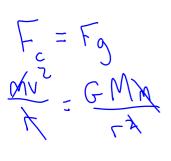
	MASS	WEIGHT
A.	decreases 🗶	decreases X
B.	decreases	increases
C.	remains constant $\checkmark$	decreases V
D.	remains constant 🗸	increases

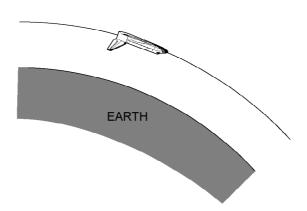
Cavendish's historic experiment is set up as shown to determine the force between two identical sets of masses. What would be the net force of attraction between **one** set of masses?



31.

A space shuttle is placed in a circular orbit at an altitude of  $3.00 \times 10^5$  m **above** Earth's surface.





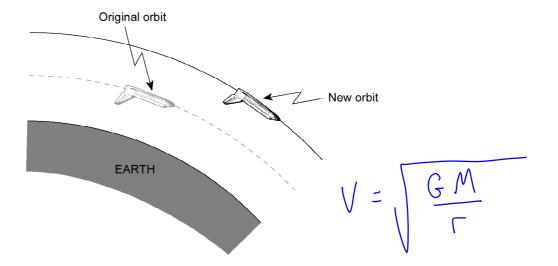
a) What is the shuttle's orbital speed?

(5 marks)

$$V = \sqrt{\frac{GM}{\Gamma}} = \sqrt{\frac{(6.67 \times 10^{-11})(5.98 \times 10^{24})}{(3 \times 10^{5} + 6.38 \times 10^{6})}}$$

$$V = 7.73 \times 10^{3} \text{ M/s}$$

b) The space shuttle is then moved to a higher orbit in order to capture a satellite.



The shuttle's speed in this new higher orbit will have to be

greater	41	• .1	1	1 .
oreater	than	in the	lower	orbit
greater	man	m unc	10 W CI	OI DIL.

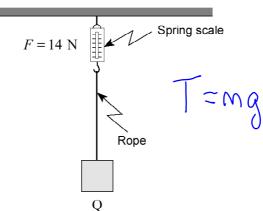
(Check one response.) (1 mark)

c) Using principles of physics, explain your answer to b).

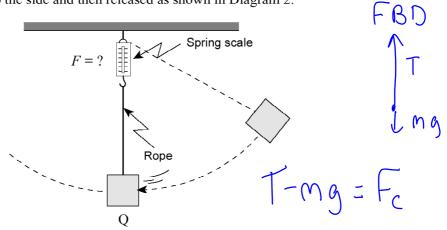
(3 marks)

V=	α5	r increases,
\\ \	V	decreases
·		

A mass is suspended by a string attached to a spring scale that initially reads 14 N as shown in Diagram 1.



The mass is pulled to the side and then released as shown in Diagram 2.



MB

As the mass passes point Q, how will the reading on the spring scale compare to the previous value of 14 N? Using principles of physics, explain your answer. (4 marks)

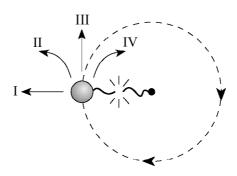
1st situation: T = Mg (see FBD above)

2nd situation: T - Mg = F (see FBD above)

T = F + Mg, which is greater than original T,

A ball attached to a string is swung in a horizontal circle.

# View from Above



Which path will the ball follow at the instant the string breaks?

A. I

B. II

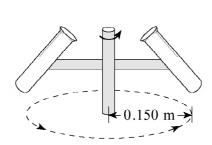
IIL

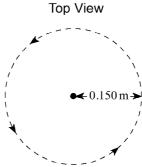
D. IV

34.

A test tube rotates in a centrifuge with a period of  $1.20 \times 10^{-3}$  s. The bottom of the test tube travels in a circular path of radius 0.150 m.

Side View

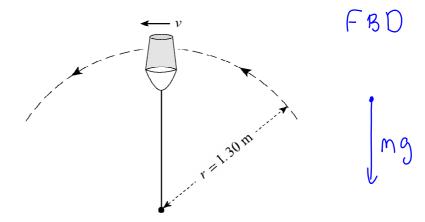




What is the centripetal force exerted on a  $2.00 \times 10^{-8}$  kg amoeba at the bottom of the tube?

A.  $9.86 \times 10^{-5} \text{ N}$ 

A physics student swings a 5.0 kg pail of water in a vertical circle of radius 1.3 m.

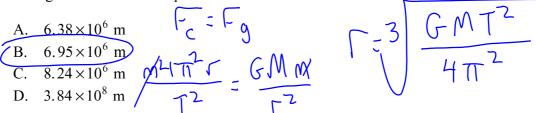


What is the minimum speed, v, at the top of the circle if the water is not to spill from the pail?

- 3.6 m/s
- we wont mg=Fc
- $6.1 \,\mathrm{m/s}$
- C. 8.0 m/s
- 9.8 m/s
- Mg = MV = Jgr

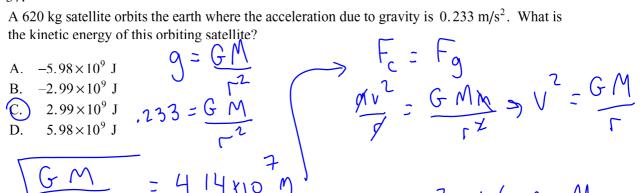
36.

Sputnik I, Earth's first artificial satellite, had an orbital period of 5 760 s. What was the average orbital radius of Sputnik's orbit?



37.

A 620 kg satellite orbits the earth where the acceleration due to gravity is 0.233 m/s<sup>2</sup>. What is



KE= 299 x 10 9 J

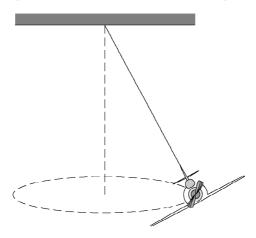
- A 5.0 kg rock dropped near the surface of Mars reaches a speed of 15 m/s in 4.0 s.
- a) What is the acceleration due to gravity near the surface of Mars? (2 marks)

$$\alpha = \frac{\sqrt{f^{-1}i}}{4} = \frac{15-0}{4} = 3.75 \text{ M/s}^2$$

b) Mars has an average radius of  $3.38 \times 10^6$  m. What is the mass of Mars? (5 marks)

$$M = \frac{7^2(3.75)}{6} = 6.412 \times 10^{23} \text{ kg}$$

A small toy airplane suspended as shown below flies in a circular path.



Which of the following free body diagrams best describes the forces acting on the airplane at the position shown?

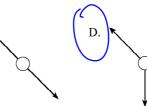
Α.



В.

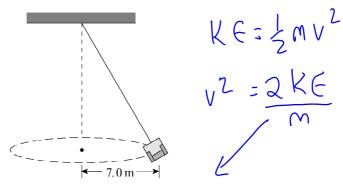


C



40.

An empty 12 kg seat on a swing-type ride at the fairgrounds has a kinetic energy of 480 J.



What is the centripetal force on the empty seat?

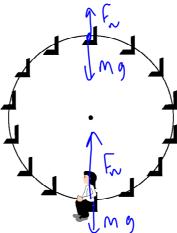
A. 
$$1.2 \times 10^2 \text{ N}$$
B.  $1.4 \times 10^2 \text{ N}$ 

C. 
$$8.2 \times 10^2 \text{ N}$$

D. 
$$5.8 \times 10^3 \text{ N}$$

A 75 kg person rides a Ferris wheel which is rotating uniformly. The centripetal force acting

on the person is 45 N.



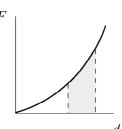
Top	$\subset$
mg-F <sub>N</sub> =	
Fn = mg - 49	)

What	force does the seat exert on the	rider at the top and at the bottom of	the ride?
	FORCE AT TOP	FORCE AT BOTTOM	1201.04
A.	690 N 🗸	690 N 🗙	F - mg = F
( B. )	690 N	780 N ✓	N My - C
C.	780 N X	690 N 🗸	FN = 45 + mg
D.	780 N →	780 N ✓	N - 13

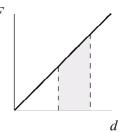
42.

Which of the following illustrates the work required to move an object in a gravitational field?

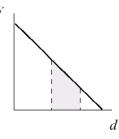
A. F

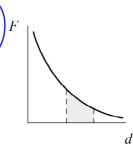


B. F



 $\mathbf{C}$ . F





A 1 500 kg satellite travels around the earth in a stable orbit with a radius of  $1.3 \times 10^7$  m.

a) What is the speed of the satellite in this orbit?

(5 marks)

$$F_{c} = F_{g}$$

$$K^{2} = \frac{GMM}{r^{2}} \rightarrow V = \sqrt{\frac{GM}{r}}$$

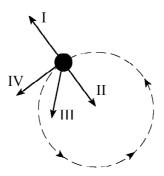
$$V = \sqrt{\frac{(G.67 \times 10^{-11})(S.98 \times 10^{24})}{1.3 \times 10^{7}}} = 5.54 \times 10^{-11} \text{ M/s}$$

The satellite is then moved to a new orbit with twice the rain this orbit is  the same as less than more than	adius of the first orbit. The speed
the speed in the first orbit. (Check one response.)	(1 mark)
Using principles of physics, explain your answer to b).	(3 marks)
V = GM as	T increases,
V	le Cre ases
	the same as less than more than  the speed in the first orbit. (Check one response.)  Using principles of physics, explain your answer to b).

### 9906

44.

A satellite moves in a circular path at a constant speed. Which vector in the diagram below best represents the satellite's acceleration?



- - D. IV

45.

A 2.5 kg object moves at a constant speed of 8.0 m/s in a 5.0 m radius circle. What is the object's acceleration?

- A.  $0 \text{ m/s}^2$

46.

What is the magnitude of Earth's centripetal acceleration as it orbits the Sun?

- A.  $1.9 \times 10^{-10} \text{ m/s}^2$
- B.  $4.2 \times 10^{-4} \text{ m/s}^2$ C.  $5.9 \times 10^{-3} \text{ m/s}^2$ D.  $9.8 \text{ m/s}^2$

$$Q_{e} = 4\pi^{2} \Gamma$$

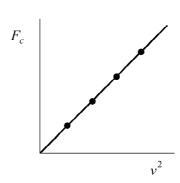
$$G_{e} = 4\pi^{2} \Gamma$$

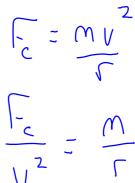
$$G_{e} = 4\pi^{2} \Gamma$$

$$G_{e} = 4\pi^{2} \Gamma$$

$$G_{e} = 7$$

A student plots a graph of centripetal force  $F_c$  versus the square of velocity  $v^2$  for an object in uniform circular motion.



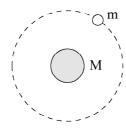


What is the slope of this graph?

- $A. \frac{m}{r}$ 
  - B.  $\frac{r}{m}$
  - $C. \quad \frac{4\pi^2 r}{T^2}$
  - D.  $\frac{T^2}{4\pi^2r}$

# 48.

Which of the following is a correct expression for the total energy of the orbiting satellite shown below?



A. 
$$E_T = -G \frac{Mm}{r}$$

B. 
$$E_T = G \frac{Mm}{r}$$

$$C. \quad E_T = \frac{1}{2} mv^2 + mgr$$

A 1500 kg satellite travels in a stable circular orbit around the earth. The orbital radius is

 $4.2 \times 10^7$  m. What is the satellite's kinetic energy?

(7 marks)

<u>Need</u> V2

Fc = Fg MV = GMM v<sup>2</sup> = GM

 $KE = \frac{1}{2}Mv^{2} = \frac{1}{2}MGM$   $KE = \frac{1}{2}(\frac{1500)(6.67 \times 10^{-11})(5.98 \times 10^{-24})}{4.2 \times 10^{-7}} = 7.12 \times 10^{-7}$ 

# Scholarship Questions. Nasty, but cool!!!!

9401

50.

An unpowered projectile is fired vertically upwards from the <u>surface of the Moo</u>n. To what height above the surface will the projectile rise if it leaves the surface at 1 500 m/s? (10 marks)

$$\frac{1}{2}mv_{0}^{2} - \frac{GMm}{G} = -\frac{GMm}{G}$$

$$\frac{1}{2}mv_{0}^{2} = -\frac{GMm}{G} + \frac{GMm}{G}$$

$$\frac{1}{2}mv_{0}^{2} =$$

A certain asteroid has a radius of  $7.0 \times 10^3$  m and a mass of  $5.0 \times 10^{15}$  kg. How fast would a cyclist have to travel on the surface of this asteroid in order for her apparent weight to be one fifth of her weight when stationary?

 $Q = \frac{GM}{(10 \text{ marks})}$ astroid  $Q = \frac{G(677)(5'')}{(5710^3)^2} = \frac{G(8067)}{(7710^3)^2}$   $Q = \frac{G(677)(5'')}{(7710^3)^2} = \frac{G(8067)}{(7710^3)^2}$ 

FOD:

$$mg - F_N = F_c$$

$$mg - mg = m\alpha_c$$

$$F_g$$

We want 
$$a_c = \frac{49}{59}$$

$$\frac{v^2}{r} = \frac{49}{59}$$

$$V = \sqrt{\frac{49}{5}} = \sqrt{\frac{4(6.806 \times 10^{-3})(7 \times 10^{3})}{5}} = 6.2 \, \text{m/s}$$

A certain planet has a radius of  $3.40 \times 10^6$  m and a mass of  $6.40 \times 10^{23}$  kg. An unpowered projectile is fired vertically upwards from the surface of this planet. To what height above the surface will the projectile rise if it leaves the surface at 1 600 m/s? (12 marks)

$$PE: + KE: = PE_{+} + KE_{+}$$

$$-\frac{GMh}{\Gamma_{i}} + \frac{1}{2}hV:^{2} = -\frac{GMh}{\Gamma_{h}}$$

$$(-6.67 \times 10^{-11})(6.4 \times 10^{23}) + \frac{1}{2}(1600)^{2} = -\frac{GM}{\Gamma_{h}}$$

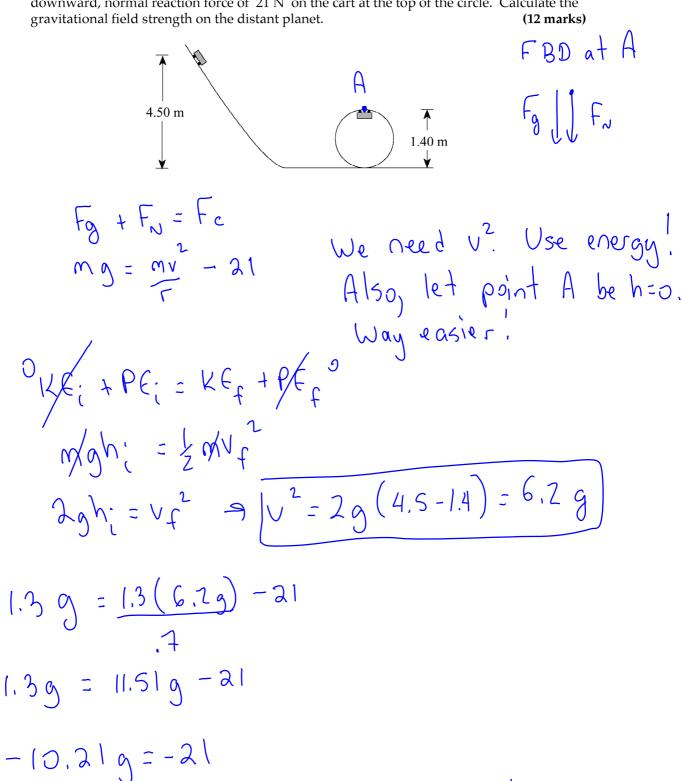
$$-1.12753 \times 10^{7} = -\frac{GM}{\Gamma_{h}}$$

$$\Gamma_{f} = (-6.67 \times 10^{-11})(6.4 \times 10^{23}) = 3.786 \times 10^{6} \text{ m}$$

$$h = \Gamma_{f} - \Gamma: = 3.786 \times 10^{6} - 3.4 \times 10^{6} = 3.86 \times 10^{5} \text{ m}$$

$$= 4.0 \times 10^{5} \text{ m}$$

A student on a distant planet performs a "loop-the-loop" experiment. She releases a frictionless, 1.3 kg cart from a height of 4.50 m. It is observed that the track exerts a downward, normal reaction force of 21 N on the cart at the top of the circle. Calculate the gravitational field strength on the distant planet. (12 marks)



q = 21/10.21 = -2.06 M/ke

# Cool question,

9508

54.

A racetrack surface has the shape of an inverted cone on which cars race in horizontal circles. For a steady speed of 29 m/s, to what distance d should a driver take her car, if she wishes to stay on a circular path without friction? (12 marks)

$$F_{N}$$
  $F_{N}$   $F_{N$ 

```
9601
55.
```

A 1500 kg satellite is in orbit 250 km above Earth's surface. What minimum additional energy

is needed to place this satellite in a new stable orbit 800 km above Earth's surface? (12 m = 
$$\frac{1}{2}$$
 =  $\frac{1}{2}$  =  $\frac{1}{2$ 

Total Energy: SPE + DKE

+ 9,024×10 = 6,941 × 10 DPE = -8,33 x 1010

$$5 \text{ KE} = \text{ kE}_{1} - \text{ kE}_{1} = \frac{1}{2} \text{ mV}_{1}^{2} - \frac{1}{2} \text{ mV}_{1}^{2}$$

$$= \frac{1}{2} \text{ mGM} - \frac{1}{2} \text{ mGM} = 4.17 \times 10^{9} - 4.51 \times 10^{9}$$

$$5 \text{ KE} = -3.4 \times 10^{9} \text{ J}$$

(6=6.94×109-3.43×109=3.5×10

#### 28. b **Answers:** 29. d 1. b 30. d 31. a) $7.73 \times 10^3$ m/s b) less than in 2. d 3. b the lower orbit c) see key 4. a 32. see key 5. b 33. c 6. a 34. c 7. 30 J 35. a 8. a 36. b 9. b 37. c 38. a) $3.8 \text{ m/s}^2$ , b) $6.5 \times 10^{23} \text{ kg}$ 10. c 11. d 39. d 12. a 40. b 13. a) $7.86 \times 10^{24} \text{ kg}$ , b) $2.72 \times 10^{10} \text{ J}$ , c) $-2.72 \times 10^{10} \text{ J}$ 41. b 42. d 43. a) $5.5 \times 10^3$ m/s b) less than c) 14. a 15. d see key 16. b 44. b 17. d 45. c 18. c 46. c 19. a) 3.61 N/kg, b) 421 N 47. a 48. d 20. a 49. 7.1 x 10<sup>9</sup> J 21. c 50. $1.2 \times 10^6 \text{ m}$ 22. d 23. d 51. 6.2 m/s 52. 4.0 x 10<sup>5</sup> m 24. d 53. g=2.06 N/kg 25. a 26. W= $1.2 \times 10^{10} \text{ J}$ 54. 130 m 27. b 55. $3.41 \times 10^9 \text{ J}$